

The reciprocal $\text{CuInS}_2 + 2\text{CdSe} \rightleftharpoons \text{CuInSe}_2 + 2\text{CdS}$ system—Part II: Liquid–solid equilibria in the system

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Abstract

The phase equilibria in the reciprocal system $\text{CuInSe}_2 + 2\text{CdS} \rightleftharpoons \text{CuInS}_2 + 2\text{CdSe}$ were investigated by differential thermal and X-ray phase analysis. The phase diagrams of a series of vertical sections, a liquidus surface projection and a spatial phase diagram were constructed. It was established that the addition of cadmium chalcogenides leads to the stabilization of the cubic modifications of the ternary compounds, which form a continuous solid solution series, at the annealing temperatures. The boundaries of the solid solutions were determined by the change of the unit cell parameters; the isothermal sections at 620 and 870 K were constructed.

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1. Introduction

The search for new efficient materials for the photo-voltaic conversion of solar energy among the complex chalcogenides remains a hot topic in the last decade [1–3]. These materials are commercially relevant by their price/efficiency ratio [4] and are already used in the industrial production of solar modules. Currently, CuInSe_2 (CIS) and $\text{CuIn}_{1-x}\text{Ga}_x\text{Se}_2$ (CIGS) have found practical application [1–3]. The efficiency of the solar radiation conversion by the thin-film elements based on these materials is 18% and 20% [1–6], respectively. Their advantage over the classic materials of the absorption layer of the solar elements (Si, GaAs) are primarily economic aspects [4] and certain specific characteristics, e.g. high radiation resistance (approximately 50 times higher) [7–9]. It is also important that the radiation damage is regenerated by their thermal processing at 470–520 K during 10–15 min [10].

The developments based on other compounds with the chalcopyrite structure are also promising (mostly CuInS_2 , e.g. [11,12]). The solid solutions based on these materials are investigated as well, in 4-element $\text{CuIn}(\text{S},\text{Se})_2$ [13,14] and 5-element $\text{Cu}(\text{In},\text{Ga})(\text{S},\text{Se})_2$ [15,16] chalcogenide phases. The major challenges in this research are the search for the optimal composition of the solid solutions and the technological improvement of thin film deposition.

There is currently no material that would fully satisfy the requirements [1,2], therefore the search for the optimal composition is a promising problem that is investigated in the latest years by a wide front of research groups.

The CuInSe_2 compound is a semiconductor of either *p*- or *n*-type conductivity (depending on the technological conditions of its production) with a bandgap energy, measured by various authors, in the 0.96–1.1 eV range [17]. The industrial production of solar cells utilizes a hetero-junction $\text{CuInSe}_2/\text{CdS}$. Though the current trend is to substitute CdS with a less toxic material, the most efficient cells were based on it [1–3]. It is known that Cu^+ ions have high diffusion coefficient [18]. Therefore, the information on possible solid-state processes (solid solubility, the

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formation of new phases) at the interface is important. This knowledge can be derived from a phase diagram of a system composed of these compounds. The $\text{CuInSe}_2\text{-CdS}$ system should be considered as an integral part of the reciprocal system $\text{CuInSe}_2 + 2\text{CdS} \rightleftharpoons \text{CuInS}_2 + 2\text{CdSe}$ that is investigated in this paper. Though the system is composed of four compounds, it is not a quaternary one because a chemical reaction is possible in the system. Such systems, according to Anosov et al. [19], belong to the chemical systems. The number of independent components in such systems equals the number of original system components (4) less the number of chemical reactions that occur in the system (1). Therefore, the number of independent components is 3 and the system is a ternary one.

An interesting benefit is a possible decrease of the cost of solar cells due to the partial substitution of indium with the solid solutions of the reciprocal system.

2. Quasi-binary systems

2.1. The CdS-CdSe system

The CdS-CdSe system is quasi-binary, type I of Roozeboom classification [20], complete miscibility, which agrees well with the fact that the compounds are isostructural. The concentration dependence of the unit cell parameters is linear [20–22].

2.2. The $\text{CuInSe}_2\text{-CuInS}_2$ system

The phase diagram of the $\text{CuInSe}_2\text{-CuInS}_2$ system was studied in [23,24]. The authors [23] established that the system was characterized by continuous solid solution series of α - and γ -solid solutions with tetragonal (low-temperature, LT, modification) and cubic (high-temperature HT(1)) structure and a region of β -solid solutions of high-temperature HT(2) modification of CuInS_2 ranging from 0 to 30 mol% CuInSe_2 . The authors [24] analyzed a possible formation in the system of two compounds that formed a continuous solid solution series between themselves and with the system components. Two phase transitions were recorded, one of which occurred in all the system alloys, whereas another one, HT(2), was typical only of alloys in the range of 67–100 mol% CuInS_2 .

2.3. The $\text{CuInS}_2\text{-CdS}$ system

In the previous work, the authors investigated the phase diagram of the $\text{CuInS}_2\text{-CdS}$ system [25]. A continuous solid solution series formed in the system between the HT(2) modification of CuInS_2 that has a wurtzite structure and CdS which is isostructural to it. Another HT(1) CuInS_2 modification that crystallizes in the sphalerite structure was stabilized at the annealing temperature by the addition of cadmium sulfide, and existed in the ~37–44 mol% CdS range at 870 K. The decrease of the

range of this solid solution at lower temperature led us to a suggestion about a possibility of a solid-state decomposition below 870 K. To confirm or disprove it, we performed an additional annealing of four alloys at 670 K. X-ray phase analysis showed that all these alloys were two-phase, containing a mixture of either tetragonal and cubic or cubic and hexagonal phases. Thus, we have confirmed the existence of the cubic phase at this temperature as well, though the homogeneity region of β -solid solutions was not determined precisely. The alloys of this region exhibited p -type conductivity and large values of thermo-EMF (~1250 $\mu\text{V/K}$).

2.4. The $\text{CuInSe}_2\text{-CdSe}$ system

The investigation of the phase diagram of this system was reviewed in the first part of this study [26].

3. Experimental

Two series of alloys were prepared for the investigation of the phase equilibria in the $\text{CuInSe}_2 + 2\text{CdSe} \rightleftharpoons \text{CuInS}_2 + 2\text{CdS}$ system, their composition and location are shown in Fig. 1. The alloys were synthesized from high-purity elements (at least 99.99 wt% purity). Calculated amounts of elements were placed into the quartz ampoules which were evacuated and soldered. At the first stage, the

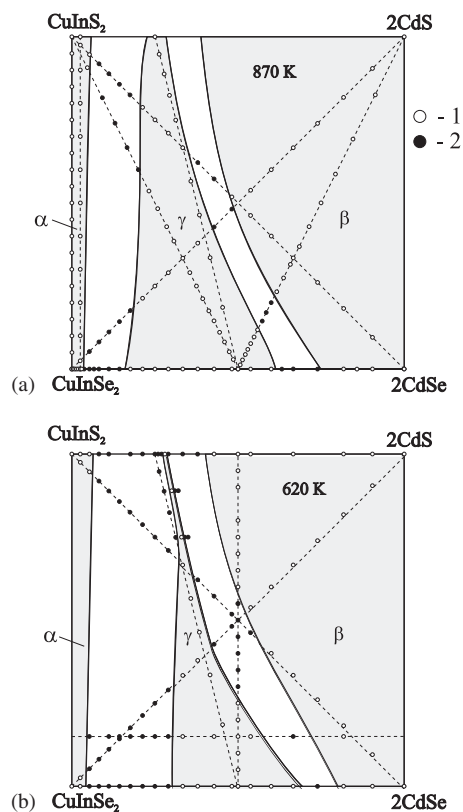


Fig. 1. Chemical and phase composition of the alloys and isothermal sections of the reciprocal system $\text{CuInSe}_2 + 2\text{CdS} \rightleftharpoons \text{CuInS}_2 + 2\text{CdSe}$ at 870 K (a) and 620 K (b) (1, single-phase alloys; 2, two-phase alloys).

Table 1
Composition of the primary phase in the alloys of the 'Cu₃Cd₂In₃S₈'–'CuCd₂InSe₄' section (EDX analysis data)

Composition, mol% 'Cu ₂ CdInSe ₄ '	Cu	Cd	In	S	Se
0	15.90	14.84	19.01	50.25	—
10	16.06	15.28	18.32	47.91	2.42
20	20.03	12.02	20.38	43.66	3.91
30	19.29	14.18	19.45	40.80	6.29
40	16.53	16.30	18.78	37.19	11.20

ampoules were heated in the oxygas burner flame to complete reaction of elementary sulfur. Then the containers were placed in the shaft-type furnace and heated at the rate of 40–50 K/h. The maximum synthesis temperature was 1420 K for all alloys. After the exposure to this temperature for 6 h with periodic vibration, the alloys were cooled (10 K/h) to the annealing temperature. The first series of the alloys were annealed for 500 h at 870 K, the second one, at 620 K during 1440 h. The annealing temperatures correspond to the upper and the lower boundaries of the temperature range of the industrial thin film deposition of the chalcopyrites in the production of the photovoltaic elements [1]. The alloys were then quenched into cold water. Obtained alloys were black compact ingots. The alloys near CuInSe₂ were typically brittle. Some alloys with high CdS content were inhomogeneous after the reported synthesis process. Those were additionally crushed into powder in an agate mortar, pressed into tablets and reheated according to the second stage of the synthesis. Obtained alloys were investigated by differential thermal (a Paulik–Paulik–Erdey derivatograph) and X-ray phase analysis (a DRON 4-13 diffractometer, CuK_α radiation). The lattice parameters were computed using PDWin-2 program package. The microstructure of polished alloys was observed at a Leica VMHT Auto microhardness tester. For the EDX analysis of the bulk samples, irregularly shaped pieces were embedded in a metacrylate matrix, polished and then examined in the scanning electron microscope (LEICA 420 I) in back-scattering mode. Cu, Cd, InAs, FeS₂, Se were used as standards. No impurity elements heavier than sodium have been observed. The experimentally determined compositions (Table 1) were close to the initial compositions of the samples.

4. Triangulation

According to the X-ray phase analysis data, the isothermal sections of the reciprocal system CuInSe₂+2CdS ⇌ CuInS₂+2CdSe contain three single-phase fields of solid solutions (Fig. 1), two of which are stretched along the side systems of the quadrangle which form the continuous solid solution series (α- and β-solid solutions), and the third one is located between them (γ-solid

solutions). The plots show that the decrease of temperature leads to narrowing of the homogeneity regions of the solid solutions. This is especially remarkable for γ-solid solutions in sulfur-rich alloys. It makes possible an assumption that at some lower temperature we should expect a decomposition by a eutectoid process of the solid solution in the CuInS₂–2CdS system in the sulfur-rich part of the quadrangle that would result in the existence of a three-phase field in that region.

The formation of γ-solid solutions means that none of the sections corresponding to the quadrangle diagonals is quasi-binary, which has its consequences in the change of the lattice parameters in the two-phase regions of the system sections. Therefore, the CuInSe₂+2CdS ⇌ CuInS₂+2CdSe system belongs, according to the classification set out in [19], to reversible reciprocal systems.

5. Results

5.1. The CuInS₂–CuInSe₂ system (Fig. 2)

Our results confirm the formation of two continuous solid solution series in the CuInS₂–CuInSe₂ system. The solid solution range of the HT(2) CuInS₂ modification is limited and decomposes by a metatectic process β ⇌ γ + L. The invariant point coordinates are 31 mol% CuInSe₂ at 1315 K (Fig. 3). The change of the unit cell parameters of the α-phase is linear.

5.2. The CuInS₂–CdS system at 620 K (Fig. 3)

As the phase diagram of this system was constructed earlier [24] during the study of the alloys annealed at 870 K, in this paper we only established the boundaries of the solid

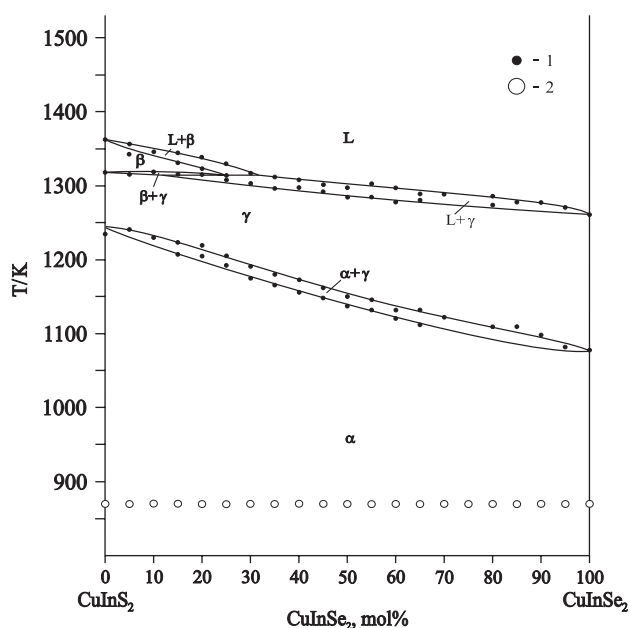


Fig. 2. Phase diagram of the CuInSe₂–CuInS₂ system (1, DTA results; 2, single-phase alloys).

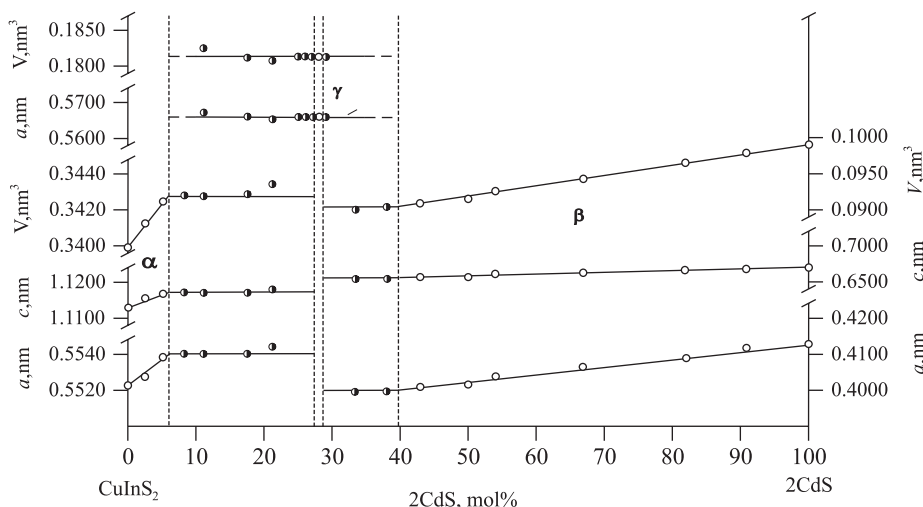


Fig. 3. Plots of the lattice parameters and unit cell volumes of the CuInS_2 – CdS section alloys at 620 K.

solutions at 620 K. The change of the lattice parameters of the system alloys at this temperature is shown in Fig. 3. The α -solid solution has a homogeneity region in the 0–6 mol% 2CdS range. The γ -phase at the annealing temperature has a minor homogeneity region that is smaller and more shifted to the CdS side than at 870 K. The solid solution range of CdS (β) at the annealing temperature extends from ~ 40 to 100 mol% 2CdS.

5.3. The ' $\text{Cu}_{0.974}\text{Cd}_{0.052}\text{In}_{0.974}\text{S}_2$ '–' $\text{Cu}_{0.974}\text{Cd}_{0.052}\text{In}_{0.974}\text{Se}_2$ ' section (Fig. 4)

The ' $\text{Cu}_{0.974}\text{Cd}_{0.052}\text{In}_{0.974}\text{S}_2$ '–' $\text{Cu}_{0.974}\text{Cd}_{0.052}\text{In}_{0.974}\text{Se}_2$ ' section (Fig. 4) is parallel to the quadrangle side CuInS_2 – CuInSe_2 ; it was necessary to establish the position of the monovariant line and to refine the homogeneity region of α -solid solution. The section liquidus is represented by one line of the primary crystallization of β -solid solution. The sub-liquidus part contains a field of secondary crystallization and a field of primary crystallization of γ -phase. Such placement of the phase fields is caused by the incongruent character of the monovariant curve (Figs. 12 and 13). At lower temperatures, the section crosses the field of γ -solid solutions, the region of the coexistence of γ - and α -phases and the field of α -solid solutions. At 870 K, all alloys are of single phase and crystallize in the chalcopyrite structure. The changes of the unit cell parameters are linear.

5.4. The ' $\text{CuCd}_2\text{InSe}_4$ '–' $\text{Cu}_3\text{Cd}_2\text{In}_3\text{S}_8$ ' section (Figs. 5 and 6)

The ' $\text{CuCd}_2\text{InSe}_4$ '–' $\text{Cu}_3\text{Cd}_2\text{In}_3\text{S}_8$ ' section is of interest because it crosses the homogeneity region of γ -solid solutions which at 870 K occupies the entire concentration range (Fig. 5). Above the annealing temperatures, the section consists of four lines, two of which correspond to the section liquidus and solidus, and two others are related to the transition from cubic \rightleftharpoons tetragonal phase. The

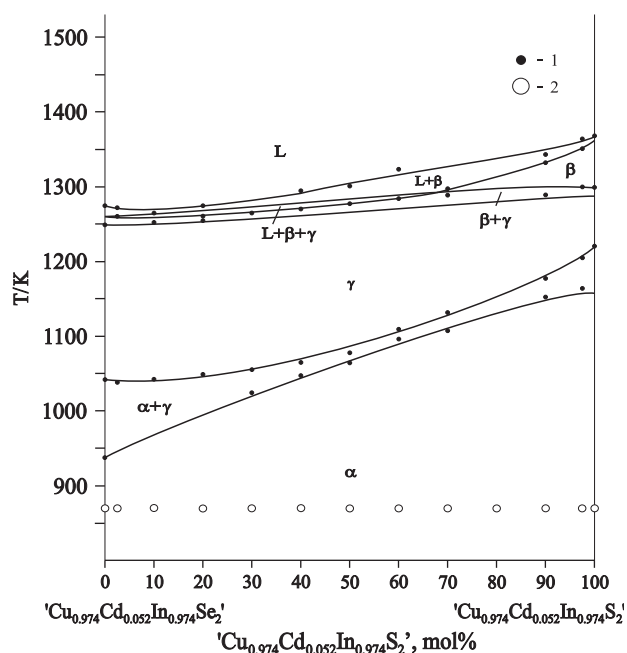


Fig. 4. Phase diagram of the ' $\text{Cu}_{0.974}\text{Cd}_{0.052}\text{In}_{0.974}\text{S}_2$ '–' $\text{Cu}_{0.974}\text{Cd}_{0.052}\text{In}_{0.974}\text{Se}_2$ ' section (1, DTA results; 2, single-phase alloys).

change of the unit cell parameters of the section alloys is shown in Fig. 6. It was discovered that at 620 K, the homogeneity region of γ -phase shifts partially to the cadmium chalcogenide-rich side, and a two-phase region ($\gamma + \alpha$) appears at the section at this temperature. EDX analysis (Table 1) of the microsections of the two-phase alloys (the composition of the prevailing phase was determined) allows us to localize the position of one of the boundaries of the γ -phase. The next step was the preparation of several additional alloys (composition and location are shown in Fig. 1b) to determine the boundaries more accurately.

5.5. The 'CuCd₂InSe₄'–'CuCd₂InS₄' section (Fig. 7)

The phase diagram of the 'CuCd₂InSe₄'–'CuCd₂InS₄' section is shown in Fig. 7. The section liquidus consists of one line that corresponds to the beginning of the primary crystallization of β -solid solutions. Its homogeneity region decreases at lower temperature, occupying at 620 K somewhat more than half of the concentration range. The formation of a phase with a cubic structure occurs instead. The $\beta \rightleftharpoons \gamma$ transition is recorded by DTA only at high

temperatures, therefore it is marked out on the diagram based on its position in the CuInSe₂–2CdSe system and on X-ray phase analysis results.

5.6. The CuInS₂–2CdSe section (Fig. 8)

The phase diagram of the CuInS₂–2CdSe section that corresponds to one of the diagonals of the concentration quadrangle is presented in Fig. 8. The liquidus and the solidus of the section are represented by the lines of the

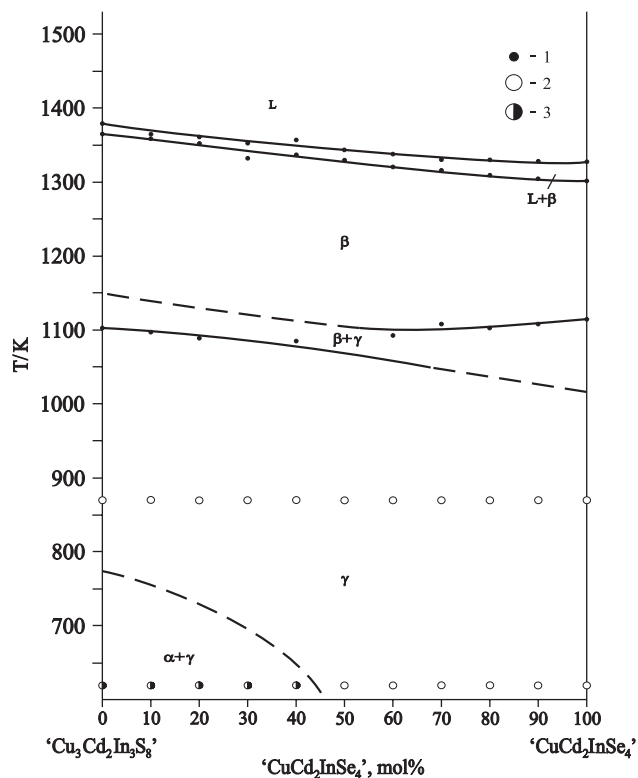


Fig. 5. Phase diagram of the 'Cu₃Cd₂In₃S₈'–'CuCd₂InSe₄' section (1, DTA results; 2, single-phase alloys; 3, two-phase alloys).

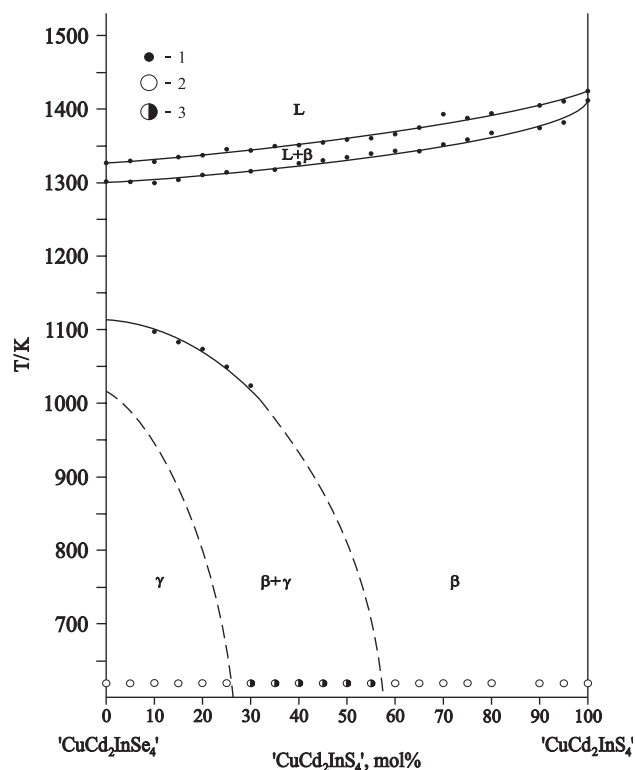


Fig. 7. Phase diagram of the 'CuCd₂InS₄'–'CuCd₂InSe₄' section (1, DTA results; 2, single-phase alloys; 3, two-phase alloys).

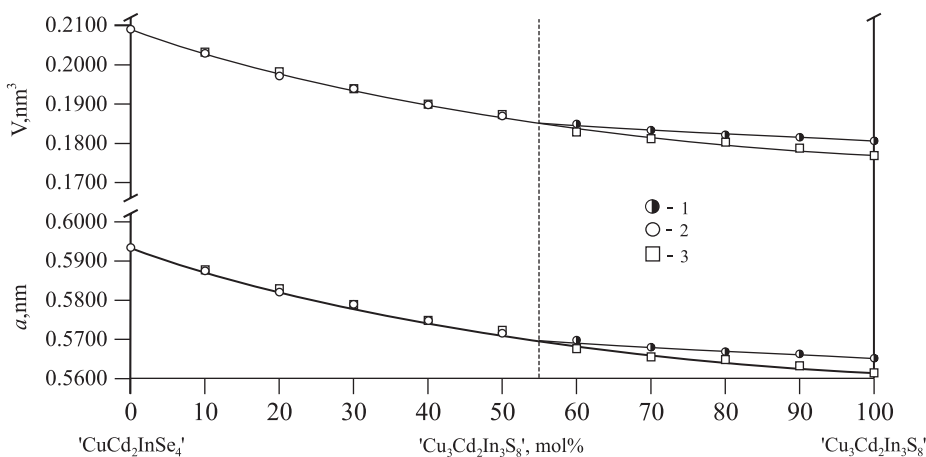


Fig. 6. Plots of the lattice parameters and unit cell volumes of the 'Cu₃Cd₂In₃S₈'–'CuCd₂InSe₄' section alloys (1, two-phase alloys at 620 K; 2, single-phase alloys at 620 K; 3, single-phase alloys at 870 K).

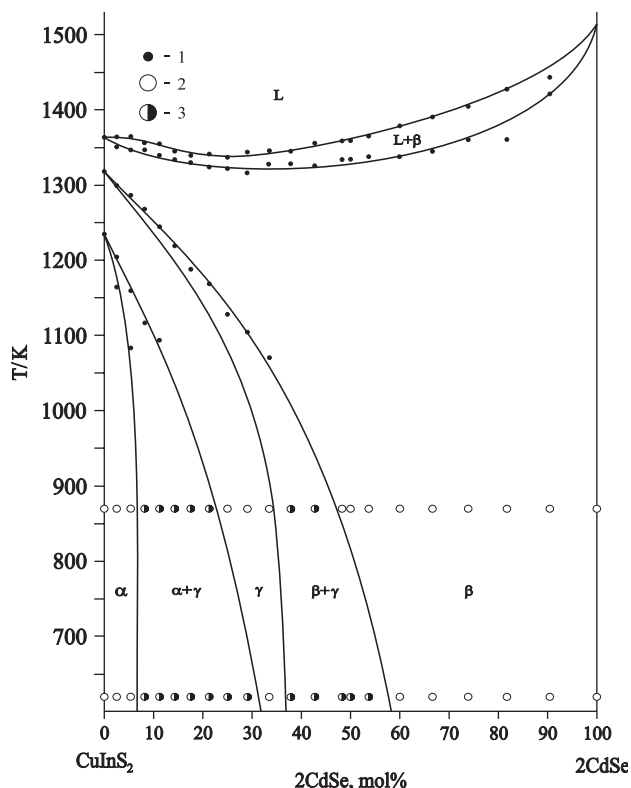


Fig. 8. Phase diagram of the CuInSe_2 – 2CdSe section (1, DTA results; 2, single-phase alloys; 3, two-phase alloys).

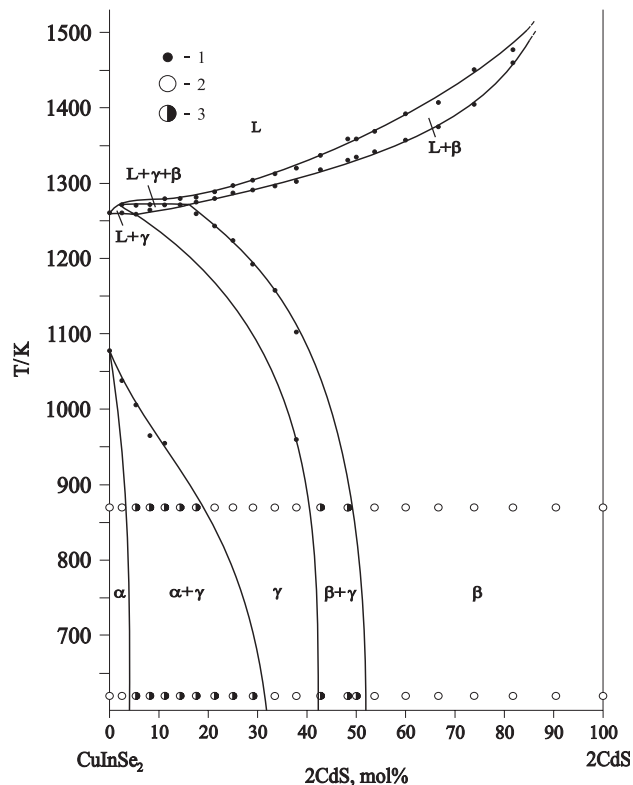


Fig. 9. Phase diagram of the CuInSe_2 – 2CdS section (1, DTA results; 2, single-phase alloys; 3, two-phase alloys).

beginning and the end of the primary crystallization of β -solid solutions; these are somewhat curved to the abscissa side. In sub-solidus part, a partial decomposition of β -solid solutions with the formation of γ -phase and, later, α -solid solutions takes place. The homogeneity regions of solid solutions were determined from the results of X-ray phase analysis of alloys annealed at different temperatures and of DTA. The XRD patterns of the alloys annealed at 620 K and 870 K contain one of three sets of diffraction reflections (that belong to the three known solid solutions) or their combination. The shift of the position of major peaks of the diffraction patterns is observed even in the two-phase region, which is reflected also in the change of the unit cell parameters of the alloys annealed at different temperatures. This means that different boundary α -, β - and γ -solid solutions are formed in different concentration ranges of the two-phase region. Therefore, the CuInSe_2 – 2CdSe section is considered non-quasi-binary.

5.7. The CuInSe_2 – 2CdS section (Fig. 9)

The CuInSe_2 – 2CdS section coincides with the other quadrangle diagonal. Its phase diagram is given in Fig. 9, and is similar to the previous one. The difference is in the extent of the homogeneity regions of the phases and the appearance of another three-phase field in the sub-liquidus part that belongs to the region of the secondary crystal-

lization of the only monovariant process that occurs in the system.

5.8. The ' $\text{Cu}_2\text{CdInSe}_4$ '– CuInSe_2 and ' $\text{Cu}_2\text{CdInSe}_4$ '– CdS sections (Figs. 10 and 11)

The ' $\text{Cu}_2\text{CdInSe}_4$ '– CuInSe_2 and ' $\text{Cu}_2\text{CdInSe}_4$ '– CdS sections were studied to establish the extent of solid solution ranges at 870 K. Both sections are described by the existence of two solid solution regions. In the former, they are solid solutions with the sphalerite and the chalcopyrite structure, in the latter, the sphalerite and the wurtzite structure. The change of the lattice parameters was observed in the two-phase region as well, therefore the solubility limits were determined by the microstructure analysis in addition to the XRD data.

5.9. The liquidus surface projection of the reciprocal system $\text{CuInSe}_2 + 2\text{CdS} \rightleftharpoons \text{CuInSe}_2 + 2\text{CdSe}$ (Fig. 12)

The liquidus surface projection of the reciprocal system $\text{CuInSe}_2 + 2\text{CdS} \rightleftharpoons \text{CuInSe}_2 + 2\text{CdSe}$ (Fig. 12) was constructed based on the literature data on the CdS – CdSe [20], CuInSe_2 – CdS [25], CuInSe_2 – CdSe [26] systems and on present results of the investigation of the above-mentioned sections. It consists of two fields of primary crystallization that correspond to β - and γ -solid solutions. The field of β -phase as the solid solution range of the phases with the

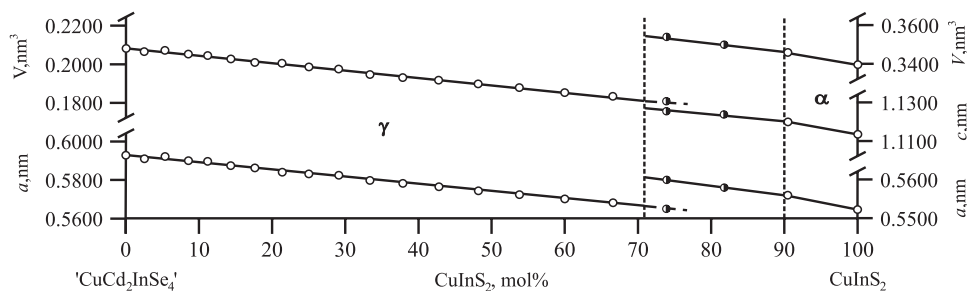


Fig. 10. Plots of the lattice parameters and unit cell volumes of the 'CuCd₂InSe₄'–CuInS₂ section alloys.

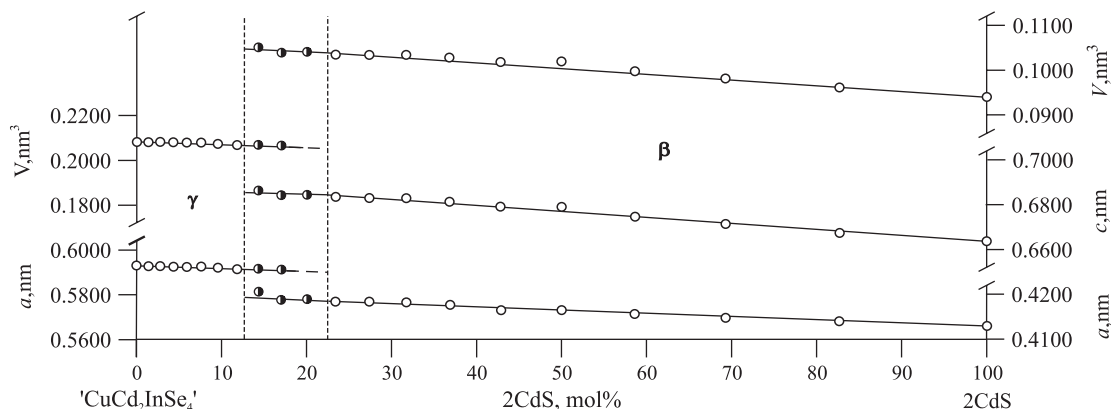


Fig. 11. Plots of the lattice parameters and unit cell volumes of the 'CuCd₂InSe₄'–2CdS section alloys.

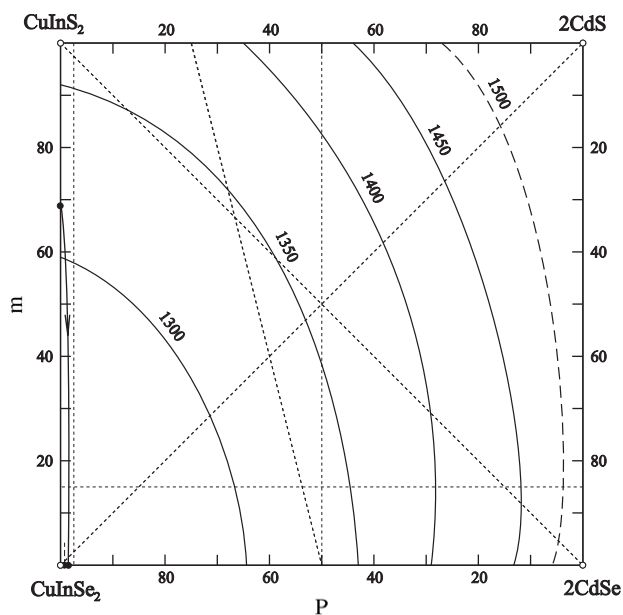


Fig. 12. Liquidus surface projection of the reciprocal system $\text{CuInSe}_2 + 2\text{CdS} \rightleftharpoons \text{CuInS}_2 + 2\text{CdSe}$.

highest melting points occupies the large part of the concentration quadrangle. The field of γ -solid solutions is minor and is localized near the quasi-binary system CuInS_2 – CuInSe_2 . The fields of primary crystallization are

separated by a monovariant line mp . The isothermal lines of the liquidus are somewhat curved to the side of cadmium chalcogenides.

5.10. Perspective representation of the $\text{CuInSe}_2 + 2\text{CdS} \rightleftharpoons \text{CuInS}_2 + 2\text{CdSe}$ system (Fig. 13)

Due to the occurrence of solid-state processes and significant solid solutions, it is advisable to consider a space version of the $\text{CuInSe}_2 + 2\text{CdS} \rightleftharpoons \text{CuInS}_2 + 2\text{CdSe}$ system (Fig. 13). Its base is a square, the edges are the compounds that form the system. Points A , B , C and D on the prism edges correspond to the melting point of the respective compounds. The prism faces are formed by the quasi-binary sections. The surface of the primary crystallization of β -solid solutions lies between points $BCDpmB$. The crystals of γ -solid solutions begin to crystallize on the surface $pAmp$. The secondary crystallization of the system is represented by one process related to the monovariant line that transforms as it goes on from a congruent ($\beta \rightleftharpoons \gamma + L$) to an incongruent one ($L + \beta \rightleftharpoons \gamma$). The volume of the secondary crystallization is limited by two horizontal lines ($m\gamma_2$ and $p\beta_3$) that lay on the bounding systems and by three lines in the middle of the reciprocal system (mp , $\beta_2\beta_3$ and $\gamma_2\gamma_1$). Based on the transformation of the processes that take place in this volume, line $\beta_2\beta_3$ should be situated above line $\gamma_2\gamma_1$. The minimum in the liquidus line that

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